# **Lesson Objectives**

1. State dimensions of a matrix.
2. Represent a linear system with an augmented matrix (and vice-versa).
3. Solve a linear system using reduced-row echelon form (rref) on calculator.
4. Determine if an ordered pair or ordered triple is a solution to a linear system of equations.
5. Solve applications with a linear system of equations and matrix rref on calculator.

**\_\_\_\_\_\_\_\_\_\_\_\_** – a rectangular array of elements, typically surrounded by large brackets

**\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_** of a matrix – \_\_\_\_\_\_\_\_ × \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ (RC)

# State the **Dimensions** of a Matrix

* **EXAMPLE:** State the dimensions of the matrix. [6.4-1]

The dimensions are: **\_\_\_\_ × \_\_\_\_**, (“two by three”) which means 2 rows by 3 columns.

# Represent a Linear System with an **Augmented Matrix** (and vice-versa)

**\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ matrix** – a matrix comprised of all coefficients and constants from a linear system written in STANDARD form.

* **EXAMPLE:** Write the augmented matrix for the system. [6.4-11]

(re-write with zeros, as needed) →

* Line up variables and constants (\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ form).
* Insert \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ as placeholders, if needed.
* Use only coefficients and constants.
* Leave behind variables and equals.
* Put large brackets on outside.
* Use vertical bar for all the equals signs.

(write as an augmented matrix) →

* **EXAMPLE:** Write the system of equations that the augmented matrix represents. [6.4-15]

(write as a linear system) →

* First column represents *x*, second is *y*, etc.
* Last column is always for the constants.
* Vertical line is for the equals signs.
* Terms with zero don’t need to be written.

# **Solve** a Linear System **Using** Reduced-Row Echelon Form **(rref) on calculator**

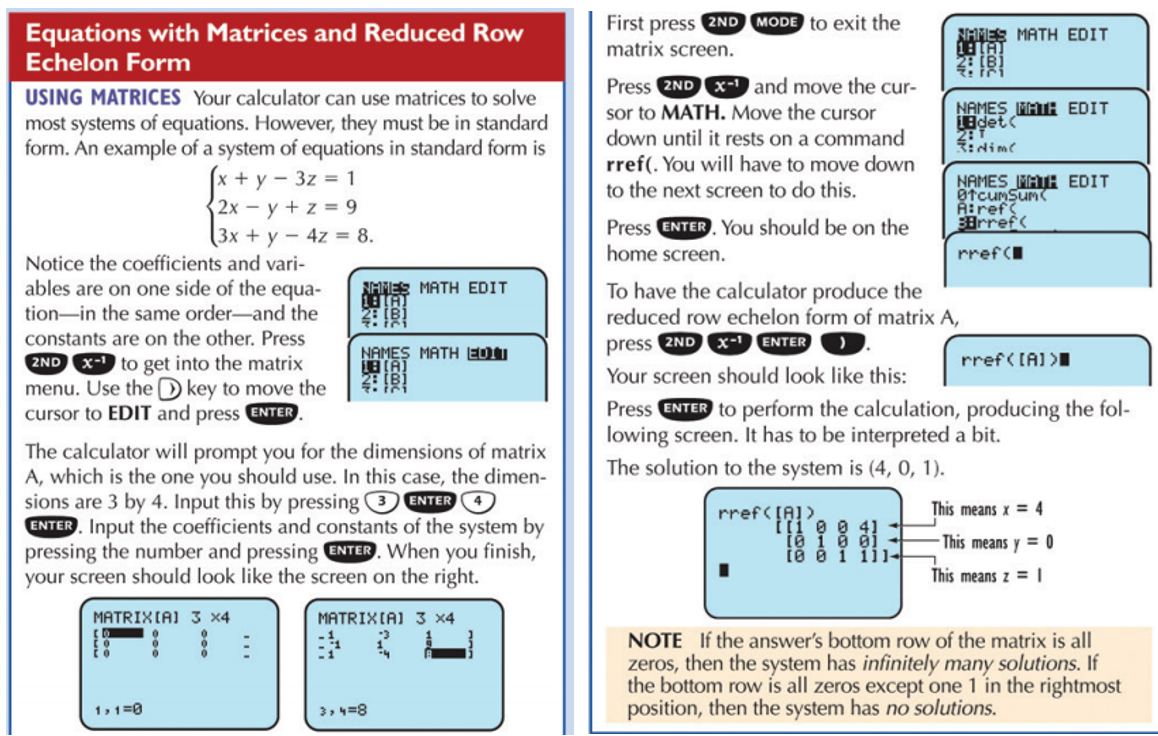
* **EXAMPLE:** The augmented matrix below is in reduced row-echelon form and represents a system of equations. If possible, solve the system. [6.4.65]

|  |  |  |
| --- | --- | --- |
| **What Reduced Row Echelon Form (rref) Looks Like** | | |
|  |  |  |
| Given rref matrix | 1’s along diagonal | Zeros elsewhere |

**Solution** is in the **LAST column** of the matrix, when in reduced row-echelon form (rref).

Translating this rref matrix back into its equation format:

(re-write as a linear system) The solution is .



* **EXAMPLE:** Use Gaussian elimination with backward substitution to solve following system of equations.

[6.4.35]

(NOTE: For the following question, solve the linear system using MATRIX method with \_\_\_\_\_\_\_\_. Do \_\_\_\_\_\_ use the Gaussian elimination method as mentioned in the directions.

So, Question Help and/or Skill Builder links will NOT be appropriate for this question.)

(write as an augmented matrix) →

Enter the augmented matrix in the calculator by pressing **\_\_\_\_\_\_\_, *\_\_\_\_\_***. (MATRIX)

The dimension of the matrix is **\_\_\_ × \_\_\_**. Enter all the values into the matrix on the calculator.

Leave the matrix by pressing **\_\_\_\_\_, \_\_\_\_** (QUIT).

Press **\_\_\_\_\_\_, *\_\_\_\_\_\_***. (MATRIX)**, \_\_\_\_** (MATH), (scroll down) **\_\_\_\_\_\_\_\_\_\_\_\_, ENTER.**

Go back into the MATRIX one last time pressing **\_\_\_\_\_, *\_\_\_\_*** (MATRIX)**, ENTER.**

 So the solution is: **( , )**

# **Determine** if an Ordered Pair (or Triple) is **a Solution** to a Linear System

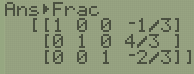
* **EXAMPLE:** Determine if the ordered triple is a solution of the system of equations.  [6.3-2]

One way to do this is similar to what we’ve done previously in Section 6.1, where we \_\_\_\_\_\_\_\_ \_\_\_\_\_ the values for *x*, *y*, and *z* from the given point into each of the three equations. The video in the homework demonstrates this as well for your reference.

A much faster way is to determine the solution by using a MATRIX with rref:

(write as an augmented matrix) →

|  |  |  |
| --- | --- | --- |
| Enter your matrix into calculator, then double-check your matrix by pressing **2ND, *x*-1**. (MATRIX)**, ENTER**.  Make corrections, if necessary. | Run the rref command on the calculator. | Press **MATH, ENTER, ENTER** to convert to fractions. |
|  |  |  |

(carried over from previous page) 

The solution given by rref is . Recall what the original problem asked:

**Determine whether the ordered triple is a solution of the system of equations.**

rref matches given point = \_\_\_\_\_\_\_\_ rref doesn’t match given point = \_\_\_\_\_\_\_

# Solve **Applications** with a Linear System of Equations

* **EXAMPLE:** There were 40,000 people at a ball game in Los Angeles. The day’s receipts were $330,000. How many people paid $12 for reserved seats and how many paid $6 for general admission? [6.1-62]

**Step 1. Define your variables.**

Let *x* = the number of \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Let *y* = the number of \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Step 2. Make your equations.**

(Total \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ equation) *\_\_\_\_\_* + \_\_*\_\_\_\_* = \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

(Total \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ equation) \_\_\_\_\_ + \_\_\_\_\_\_= \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Step 3. Convert equations to an augmented matrix.**

(write augmented matrix) →

**Step 4. Enter augmented matrix (2 × 3) into calculator and do rref to get solution.**

|  |  |
| --- | --- |
| Confirm your augmented matrix | Compute rref ( [ A ] ) |
|  |  |

**Step 5. Interpret your rref ( [ A ] ) solution correctly in context for the answer.**

The solution is (15000, 25000), which means *x* = 15,000 and *y* = 25,000.

**\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ people purchased $12 reserved seats**

**\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_ purchased $6 general admission.**

Sources Used:

1. Calculator Review Card, page 6 – Equations with Matrices and Reduced Row Echelon Form <https://media.pearsoncmg.com/aw/aw_mml_shared_1/calculator_review_card.pdf>
2. Pearson MyLab Math *College Algebra with Modeling and Visualization, 6th Edition*, Rockswold
3. Wabbitemu calculator emulator version 1.9.5.21 by Revolution Software, BootFree ©2006-2014 Ben Moody, Rom8x ©2005-2014 Andree Chea. Website <https://archive.codeplex.com/?p=wabbit>